
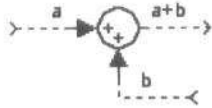
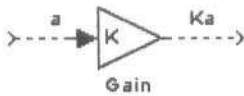



1. (10%) Develop a block diagram representation of each of the coming dynamic systems by using only the following block units

integration block:		summing block:	
scalar gain block:		mathematic function block:	

Note that when using the scalar gain or the mathematical function block, you are required to specify the gain value or the mathematical function you desire.

1a. (5%)  $\ddot{y} + 4\dot{y} + 3y = u$

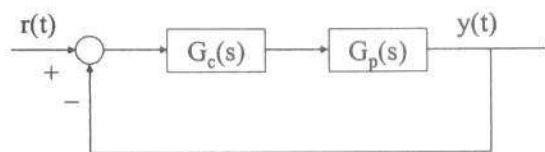
1b. (5%)  $\ddot{y} - 2y + y^3 = u$   
 $u = -5y - \dot{y}$

2. (15%) Consider the following dynamic system

$$\ddot{y} + 4\dot{y} + 3y = u$$

- 2a. (5%) With  $y(0) = 1$ ,  $dy(0)/dt = 0$ , and  $u(t) = 0$  for all  $t \geq 0$ , use the Laplace transform method to solve for  $y(t)$ .
- 2b. (5%) With  $y(0) = 1$ ,  $dy(0)/dt = 0$ , and  $u(t) = 1$  for all  $t \geq 0$ , find  $\lim_{t \rightarrow \infty} y(t)$ .
- 2c. (5%) In 2b, will  $\lim_{t \rightarrow \infty} y(t)$  depend on the initial values,  $y(0)$  and  $dy(0)/dt$ ? Why?

3. (25%) Consider the following feedback control system

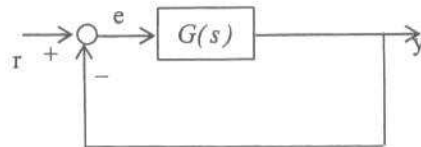


where  $G_p(s) = \frac{1}{s(s+1)}$  and  $G_c(s)$  a feedback controller.

- 3a. (5%) Assume  $G_c(s)$  is a proportional control. Determine the root locus of the closed-loop system as the proportional gain varying.
- 3b. (10%) Consider the case where  $G_c(s)$  is a PD (proportional-derivative) control. Use this example to elaborate the effect of the addition of an extra zero on the closed-loop root locus.
- 3c. (10%) Consider the case where  $G_c(s)$  provides an additional pole, e.g.,

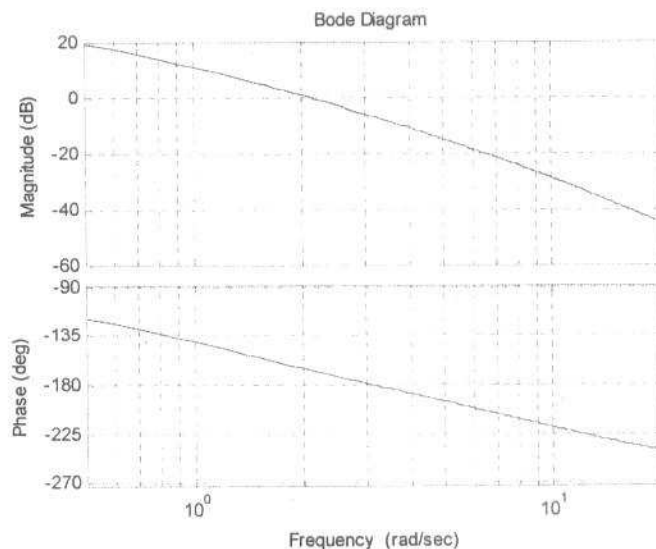
$G_c(s) = \frac{K}{s+p}$ . Use this example to elaborate the effect of the addition of an extra pole on the closed-loop root locus.

4. (25%) Given a unit feedback system as shown in the figure below, where  $r$  is the reference,  $y$  the output, and  $e$  the error.

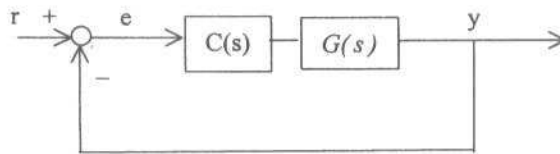


The transfer function  $G(s)$  and its Bode plot are given as follows.

$$G(s) = \frac{50}{s(s+1)(s+10)}$$



- 4a. (5%) Please plot the Nyquist Diagram of  $G(s)$ .
- 4b. (5%) From the Bode plot, determine the gain margin, phase margin, and crossover frequency.
- 4c. (5%) Use the information in (b), find the approximate settling, and damping ratio for the closed loop system
- 4d. (10%) Determine the gain margin using analytical method and compare the result obtained from (b)
5. (25%) Consider a closed loop system as shown below where  $G(s)$  is a plant and  $C(s)$  a controller.



The transfer function of  $G(s)$  is given as

$$G(s) = \frac{1}{s(s+10)}$$

and the controller is assumed to be in the following form

$$C(s) = K \frac{1+s/z_0}{1+s/p_0}$$

The specifications of the closed loop system are:

- (i) the damping ratio of the dominant root of the closed loop system to be 0.45, and
  - (ii) the velocity error constant equal to 100.
- (a) (10%) Plot the asymptotic approximate Bode diagram of the  $G(s)$
- (b) (5%) Will you choose a lead or a lag controller for  $C(s)$ ? Explain why?
- (c) (10%) Find the parameters  $K, z_0, p_0$  of  $C(s)$  to meet the specifications.