

1. (50%) Consider a unity negative feedback system as shown in Fig. 1. The Bode plot of the open loop system  $G(s)$  is shown in Fig. 2. Please answer the following questions regarding the performance of the closed-loop systems.

- (a) (10%) Please estimate the phase margin and gain margin of the system.
- (b) (5%) Please estimate the bandwidth of the system.
- (c) (5%) Please estimate the steady-state error due to unit step input.
- (d) (10%) Please estimate the percent overshoot due to unit step input.
- (e) (10%) Please estimate the damping ratio of the system.
- (f) (10%) Please plot the corresponding Nyquist plot of  $G(s)$ .

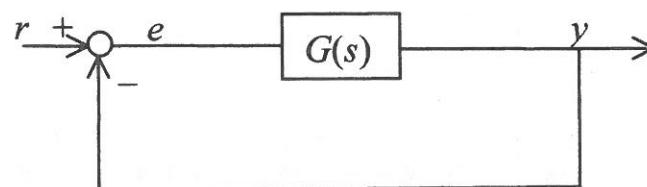


Fig. 1

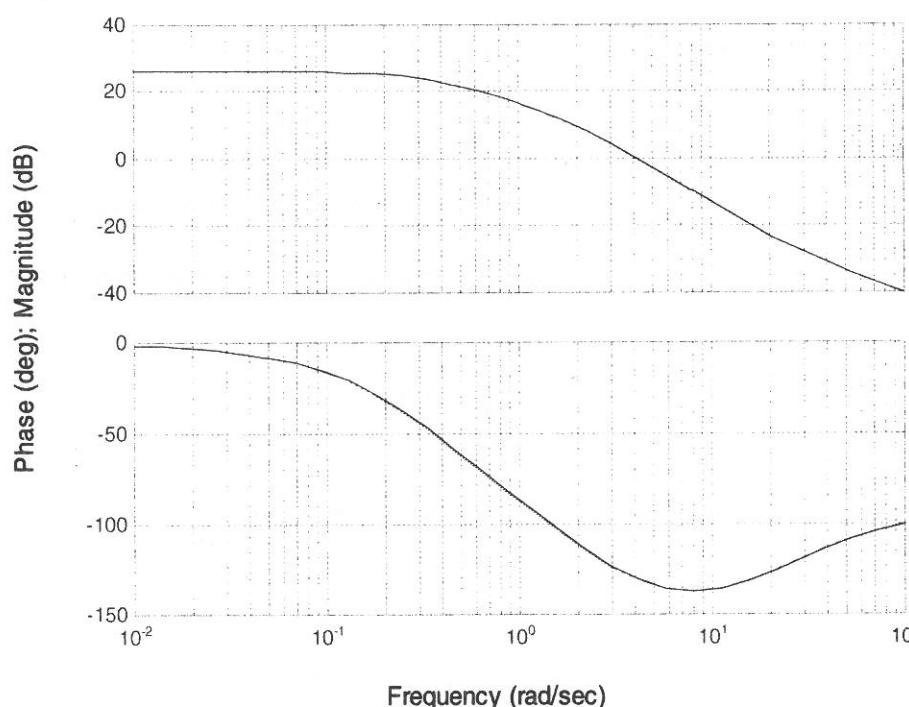
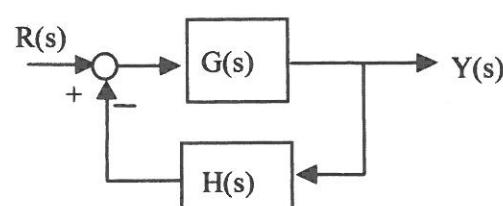


Fig. 2

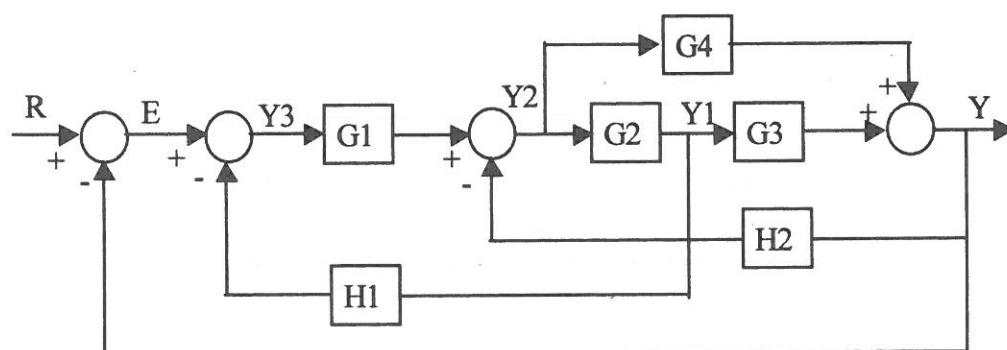
2. (20%)  $G(s) = \frac{s}{s^2 + 2s + 1}$ ,  $H(s) = \frac{1}{s}$



(a) Find the closed-loop transfer function  $M(s)$ .

(b) Find the sensitivity function  $S_G^M$ .

3. (10%) Using Mason's rule, find the closed-loop transfer function  $Y/R$ .



4. (20%) For the unity-feedback control system  $G(s) = \frac{500}{s(s+50)(s+200)}$ ,

determine the step-, ramp-, and parabolic-error constants, and the steady-state error for a unit-step input  $u_s(t)$ , a unit-ramp input  $tu_s(t)$ , and a parabolic input

$(t^2/2)u_s(t)$ , respectively.